## Mark schemes

1. (a) (Work done $=$ lost $\left.\mathrm{KE}=1 / 2 m v^{2}=\right) 0.019$ (J) $\checkmark$
(b) Use of $W=F s \checkmark$ $(F=) 0.66(N) \checkmark$

Condone POT error in substitution
ECF from (a)

## Alternative:

Use of an appropriate suvat equation and use of $F=m a \checkmark$
$\left(t=9.8 \times 10^{-6} \mathrm{~s}\right)$
( $a=6.0 \times 10^{8} \mathrm{~m} \mathrm{~s}^{-2}$ )
Condone POT error in substitution
No ECF from 3.1 this route $(F=) 0.66(N) \checkmark$
(c) Use of Volume $=$ Thickness $x$ area of cross-section $\checkmark$

Condone POT errors apart from final answer $(V=) 8 \times 10^{-4} \times 0.03$ $\operatorname{Or}(V=) 2.4 \times 10^{-5}$
(Average density $=\frac{50+5}{2}=27.5 \mathrm{~V}$
Use of density $=\frac{\operatorname{mass}}{\text { voume }}$
Condone use of their density and volume
$($ mass $=) 6.6 \times 10^{-4}(\mathrm{~kg}) \checkmark$ c.a.o

## Alternative:

Use of Volume $=$ Thickness $x$ area of cross-section $\checkmark$
Condone POT errors apart from final answer

$$
(V=) 8 \times 10^{-4} \times 0.03 \operatorname{Or}(V=) 2.4 \times 10^{-5}
$$

Use of density $=\frac{\text { mass }}{\text { voume }} /($ mass $=) 1.2 \times 10^{-3}$ or $1.2 \times 10^{-4} \checkmark$
(Average mass $=) \frac{1.2 \times 10^{-2}+1.2 \times 10^{-4}}{2} \checkmark$
$=6.6 \times 10-4(\mathrm{~kg}) \checkmark$ c.a.o
Condone use of their density and volume ( $50 \mathrm{~kg} \mathrm{~m}^{-3}=1.2 \times 10^{-3}$ )
$\left(5 \mathrm{~kg} \mathrm{~m}^{-3}=1.2 \times 10^{-4}\right)$

## Alternative:

Condone POT errors apart from final answer
Attempts to determine the area under the graph:
Formula for area of a rectangle added to the formula for area of a triangle seen / formula for the area of trapezium seen $\checkmark$

$$
\begin{aligned}
& 5 \times 0.03+\frac{(50-5) \times 0.03}{2}=0.825\left(\mathrm{~kg} \mathrm{~m}^{-2}\right) \\
& \text { or } \frac{50+5}{2} \times 0.03=0.825\left(\mathrm{~kg} \mathrm{~m}^{-2}\right)
\end{aligned}
$$

Multiplies their area by $8 \times 10^{-4} \checkmark$
Mass $=6.6 \times 10^{-4}(\mathrm{~kg}) \checkmark$ c.a.o
(d) $\mathbf{Q}$ has a larger volume (for the same mass and KE) /
$\mathbf{Q}$ has a larger surface area (for the same mass and KE) $\checkmark$
$\mathbf{Q}$ will experience a greater resistive force (at any given speed) / $\mathbf{Q}$ will displace more matter per unit distance $\sqrt{ }$
$\mathbf{Q}$ will do more work per unit distance / $\mathbf{Q}$ will transfer more of its kinetic energy per unit distance / $\mathbf{Q}$ will experience a greater deceleration $\checkmark$

Must have $\mathbf{Q}$ will travel a shorter distance for all 3 marks.
$2 .{ }^{B}$

$$
\sqrt{2} v
$$

3. D

$$
\frac{m v^{2}}{2}
$$

4. Only total momentum is conserved.
5. (a) Closed triangle of forces drawn $\checkmark$

Appropriate scale $\checkmark$
$\theta=23$ to $27\left({ }^{\circ}\right) \checkmark$
$U=77$ to 81 (N) $\checkmark$
Accept scale where 10 N is represented by at least 1 cm .


Treat each marking point independently.
Do not accept answers for $U$ and $\theta$ without a scale diagram.
Maximum of 3 marks for a free-body diagram where forces have been drawn to scale. (Check figure 8)
(b) $\quad V$ is vertical / Force at $\mathbf{Y}$ is now vertical / $V$ does not have a horizontal component / $V=S+31$ / $V$ is perpendicular to the pole / $V$ is of greater magnitude than $U /$ Force at $\mathbf{Y}$ has increased in magnitude $\sqrt{ }$
(Because) $S$ and weight (or $m g$ ) are both vertical (in Fig 3) $\checkmark$
(Because) greater moment of weight (about $\mathbf{Y}$ ) in Fig $\mathbf{3}$ / smaller moment of weight (about $\mathbf{Y}$ ) in Fig 1 / (Because) $S$ is larger in magnitude than $D$ (to produce a greater moment (about $\mathbf{Y}$ because they are equal distances from Y) $\sqrt{ }$
6. (a) Use of $p=m v$ or estimates walking speed $=1$ or $2 \mathrm{~m} / \mathrm{s} \checkmark$

Allow use of where $m$ has been made the subject and $p$ has been substituted.

Accept any answer in range $2 \times 10^{6}$ to $10 \times 10^{6}(\mathrm{~kg}) \checkmark$
Range on answer:
(Using speeds in range $0.5 \mathrm{~ms}^{-1}$ to $2.5 \mathrm{~ms}^{-1}$ )
Accept 1 significant figure answer
(b) Max 4

There is a force on the water (from the propeller) and this produces an equal force on the propeller (from the water in the opposite direction) $\checkmark$ Correctly links to Newton's $3{ }^{\text {rd }}$ law $\checkmark$

This force on the ship equals the drag force on the ship $\checkmark$ Correctly links to Newton's 1st law $\checkmark$

Force is needed to change the water's momentum $\checkmark$ Correctly links to Newton's $2^{\text {nd }}$ law $\sqrt{ }$

Must link correct law to at least one correct statement for all 4 marks
(c) (When system is enabled,) drag decreases by more than thrust

Or
(When system is enabled,) decrease in work done (per second) against drag (at any speed) is greater than the decrease in the work done by the propeller (at any rotational speed) $\sqrt{ }$

Work done (per second) by drag decreases and work done (per second) by propeller decreases (at any rotational speed)

To maintain constant momentum then drag must equal thrust $\checkmark$
Propeller can operate at lower rotational speed so that thrust again equals drag
Or
Engine does less work (and less fuel needs burnt) $\checkmark$
3rd MP: Accept answer in terms of power $=F v$
7. ${ }^{C}$


8 . $B$
190 m
9. (a) arrow between block and belt pointing upwards along the belt
(b) $\quad(F=) 19 g \sin 23^{\circ}$ to give $72.8(\mathrm{~N}) \checkmark$

Allow 2 sf answer.
(c) uses $F=\frac{\Delta(m v)}{\Delta t}$

Allow for MP1 use of appropriate kinematic equation for a AND use of $F=m a$
$F=12(\mathrm{~N}) \checkmark$
their $(\mathrm{b})+12(\mathrm{~N}) \checkmark$
(d) uses $V$ and $I$ to get total input power or energy $\checkmark$

$$
\begin{aligned}
& P_{\text {input }} \text { of motor }=110 \times 5.0=550 \mathrm{~W} \\
& E_{\text {input }}=550 \times \frac{8.0}{0.32}=13750 \mathrm{~J}
\end{aligned}
$$

uses efficiency equation $\checkmark$

$$
\begin{aligned}
& P_{\text {useful }} \text { to belt }=550 \times 0.28=150 \mathrm{~W} \\
& E_{\text {useful }}=3850 \mathrm{~J}, \text { from } 154 \times \frac{8.0}{0.32} \text {, or } 13750 \times 0.28
\end{aligned}
$$

determines power or energy to move one block $\checkmark$

$$
\begin{aligned}
& P_{\text {block }}=22 \text { or } 23 \mathrm{~W} \\
& E_{\text {block }}=560 \text { or } 580 \mathrm{~J}
\end{aligned}
$$

divides (total) useful power or energy by individual power or energy to give answer of 6 blocks $\checkmark$

Allow ecf for MP4 only for their (c)
[9]
10.
moving up with a decreasing velocity.
11. C

$$
80 \mathrm{~m} \mathrm{~s}^{-1}
$$

12. C

The acceleration of $\boldsymbol{X}$ is the same as that of $\boldsymbol{Y}$.
13. C

The terminal speed of $\boldsymbol{Y}$ is greater than that of $\boldsymbol{Z}$.
14. (a) horizontal velocity $=20 \cos 40^{\circ}=15.3 \checkmark\left(\mathrm{~m} \mathrm{~s}^{-1}\right)$

Needs minimum 3 sf
For MP1 it must be clear that the horizontal velocity has been determined.
horizontal velocity (is constant) / minimum when vertical velocity $=0 \checkmark$
(b) (vertical velocity) $v=20 \sin 40^{\circ}(=12.9) \checkmark\left(\mathrm{m} \mathrm{s}^{-1}\right)$
$s=u t+\frac{1}{2} a t^{2}$
$-3=-12.9 t+\frac{1}{2} \times 9.81 t^{2}$ or $3=12.9 t-\frac{1}{2} \times 9.81 t^{2} \checkmark$
$\left(4.91 t^{2}-12.9 t+3.00=0\right)$
For second mark both suvat equation and substitution must be shown. Equation may be rearranged before substitution
(c) Use of quadratic formulae with,+- or $\pm \checkmark$

$$
\text { eg } t=\frac{12.9 \pm \sqrt{(-12.9)^{2}-4 \times 4.91 \times 3.00}}{2 \times 4.91}
$$

0.258 s and $2.37 \mathrm{~s} \checkmark$

Two correct answers alone scores first 2 marks.
Time to reach 3 m once on the way up and once on the way down (OWTTE) $\sqrt{ }$
Larger value $\checkmark$
ecf available for last 2 marks
(d) $s=v t=20 \cos 40^{\circ} \times 2.37=36.3 \mathrm{~m}$ so no $\checkmark$
ecf from (c)
Calculation must be seen
(e) Gradient is the acceleration AND
area under graph $=\underline{\text { vertical }}$ distance travelled $\boldsymbol{V}_{1}$
Without air resistance:
comment about gradient $\sqrt{ } 2$
comment about area $\sqrt{3}$
With air resistance
comment about gradient $\checkmark_{4}$
comment about area $\sqrt{5}$
For each comment on the graph a reason must be given not just a description.
e.g for $\sqrt{ }{ }_{2}$

- constant gradient $=g$ or $9.81 \mathrm{~m} \mathrm{~s}^{-1}$
e.g. for $\checkmark_{4}$
- initially steeper gradient since air resistance in same direction as weight (so $a>g$ )
- when line crosses time axis, gradient $=g / 9.81 /$ gradient without air resistance as air resistance $=0$ when $v=0 /$
- After crossing time axis, gradient decreases as air resistance increases with speed


## E.g. for $\sqrt{3}$ or $\sqrt{5}_{5}$

- total area under graph $=0$ since ball starts and finishes on ground
- area between graph and axis is max height/vertical distance
- without air resistance reaches a higher height as area greater statement referring to area under both graphs gains $\checkmark_{3}$ and $\checkmark_{5}$

15. D 9.6 N
16. C

17. G $F$
18. C

250 J
19. A
the acceleration of the car increases.
20. (a) Use of $E_{\mathrm{k}}=1 / 2 m v^{2} \checkmark$
(Kinetic energy =) $9.2 \times 10^{9}(\mathrm{~J}) \checkmark$
Condone POT error on $1^{\text {st }} \mathrm{MP}$
Allow use where $v$ where has been converted from $5.5 \mathrm{~km} \mathrm{~h}^{-1}$
An answer to 2 significant figures (with some working) $\checkmark$
Significant figure mark requires evidence of some relevant working.
(b) Why force on the gas:

The gas's momentum is changing
This require a force according to Newton's $2{ }^{\text {nd }}$ law $\checkmark$
Or
The gas is being accelerated $\checkmark$ This require a force according to Newton's 2 nd law $\checkmark$

## Max 3 for why there is a force on the gas and why there is a resistive force on the system

Must have why the system decelerates to obtain all 4 marks.
The reason why the resultant force causes the deceleration rather than the acceleration.

Why (resistive) force on system:
The gas exerts a force on the parachute (with an equal magnitude and opposite direction force) / there is air resistance (on the system) / there is drag (on the system) / there is a resistive force (on the system) $\checkmark$
(because) the Parachute exerts a force on the gas according to Newton's $3^{\text {rd }}$ law $\checkmark$
Allow statement that is equivalent to N1 / N2 / N3.
Allow: air resistance (or drag) increases.
Allow: there is an upward force
must have a clear action-reaction pair for this N3 mark.

## Why system decelerates:

The resistive force is greater than the weight so there is a resultant force Or
The resultant force is acting in the opposite direction (to its motion). $\checkmark$
acceleration in same direction as resultant force according to Newton's 2 nd law $\checkmark$ allow the resultant force is vertically upwards
Or
Links to violation for conditions of Newton's $1^{\text {st }}$ law and therefore cannot continue at constant velocity.
(c) Attempt at determining difference $=3.3\left(\times 10^{5}\right)-2.2\left(\times 10^{5}\right)$ or difference $=1.1$ $\left(\times 10^{5}\right) \checkmark$
$1^{\text {st }}$ mark: Credit an application of conservation of energy (allow written statement, or equation without substitution)
Ignore signs on difference and answer.
MP2 allow their energy in a substitution that is, otherwise correct.
Condone an answer $=18.4\left(\mathrm{~m} \mathrm{~s}^{-2}\right)$ is worth 2 marks.
Use of $E_{p}=m g h \checkmark$
$(\mathrm{g}=) 3.7\left(\mathrm{~m} \mathrm{~s}^{-2}\right) \checkmark$
Condone $m g h=1 / 2 m v^{2}$ where rearranged to make $g$ subject.
Condone $610 \times g \times 49=$ their energy
Alternative:

- Attempt to use appropriate equations of motion to determine acceleration
$v^{2}=u^{2}+2$ as rearranged to make a the subject (condone use of their values for $v$ and $u$ and $/$ or $g=a$ )
- Attempt to use $W=F s$ to determine the air resistance $F_{D}$ (or $F_{D}=6734(.7)$ ( $N$ ) seen)
- Attempt to determine $g$ from the deceleration of the system

$$
g=\frac{F_{D}-m a}{m}
$$

(d) More mass to displace / more particles to collide with / more gas / dust to displace $\checkmark$

Must have some interaction with parachute-spacecraft.
N/E to say there are more particles / gas / dust /mass
(at any given speed)
Greater (rate of) change of momentum / More work done (per unit distance) / Greater (resistive) force / more kinetic energy transferred (per unit distance) $\checkmark$

Greater resultant force on the system (therefore greater deceleration) / greater loss of velocity per second (therefore greater deceleration) $\checkmark$
$3^{\text {rd }}$ MP for greater resultant force: allow the idea that the difference between the drag and weight has increased
$3^{\text {rd }}$ MP
Allow clear statement that links:

- rate of change of momentum of gas / dust to rate of change of momentum of system
- rate of work done on gas / dust to rate of work done by system
(a) Use of an appropriate equation of motion $\checkmark$

Where $v^{2}=u^{2}+2$ as is correctly stated, condone one error in substitution e.g. sign of a
Where other equations are used it must be clear that $v$ can be determined.
Must see $v$ as subject and an attempt to determine $t$.
$(\mathrm{v}=) 0.35\left(\mathrm{~m} \mathrm{~s}^{-1}\right) \checkmark$
Allow more than 2 sf where correct.
(b) Use of $\tan 35=\mathrm{u}_{\mathrm{v}} / 8.8$

Or
Use of $u \cos 35=8.8$ and $u_{v}=u \sin 35$
and
6.2 or 6.16 with supporting a calculation $\checkmark$

Alternative: credit use of sine rule
Must see answer to at least two significant figures
(c) Use of an appropriate equation of motion $\checkmark$ ECF

Condone their incorrect value of $u$ in this substitution.
Condone errors in signs in substitution Where other equations are used it must be clear how $t$ can be determined.
Must see $t$ as subject and an attempt to determine $s$.
( $\mathrm{t}=$ ) $0.63(\mathrm{~s}) \checkmark \quad \mathrm{ECF}$
0.61 (s) for use of $u=6 \mathrm{~m} \mathrm{~s}^{-1}$

For MP2, where their value of $u$ is used, the answer must be consistent with this value. Only allow this use where their value of $u$, to 1 significant figure, $=(5<u<7) \mathrm{m} \mathrm{s}^{-1}$ Condone 1 significant figure answer where $U$ is 1 sig fig.
(d) Use of an appropriate equation of motion $\checkmark$ ECF

Where equation is correctly stated, condone one error in substitution e.g. one error on sign of a substituted value or one incorrect value substituted (of course, ecf is acceptable)
$(\mathrm{h}=) 1.9(\mathrm{~m}) \checkmark \quad$ ECF
$h=1.83 \mathrm{~m}$ for use of $u=6 \mathrm{~m} \mathrm{~s}^{-1}$ allow ecf on $t$ (check (c))
For MP2, where their value of $u$ is used, the answer must be consistent with this value. Only allow this use where their value of $u$, to 1 significant figure, $=(5<u<7) \mathrm{m} \mathrm{s}^{-1}$ allow reverse calculation where $u=0$ and $v=6 \mathrm{~m} \mathrm{~s}^{-1}$
23.

C

24 D
25. C
26. B
28. A
29. B
30. (a) Evidence of distance travelled $=$ area under graph $=1755+1440+1620=4815 \checkmark$ Full marks can be credited for use of suvat.

Average speed $=$ total distance/time taken $=4815 / 240$
$=20.1 \mathrm{~m} \mathrm{~s}^{-1} \checkmark$ (at least 3sf)
Which is less than (speed) limit, (and therefore the answer is No). $\checkmark$
Allow ecf for distance in MP2
Only award MP3 for incorrect speed if attempt made to calculate distance correctly e.g. area under graph OR a.e. in distance or speed

Alternative for MP2 and MP3
Calculation of distance travelled at speed limit $=5280 \mathrm{~m} \checkmark$
Which is greater than distance travelled (so no). $\checkmark$
Alternative for MP1 and MP2:
Total area $=80.25 \mathrm{~m} \mathrm{~s}^{-1} \min \checkmark$
Time $=4 \mathrm{~min}$
Average $=20.1 \mathrm{~m} \mathrm{~s}^{-1} \checkmark$
(b) Using reaction time of $2.0 \mathrm{~s} \checkmark$

Use of distance $=$ speed $\times$ time $=62 \mathrm{~m}$.
62 m (would be appropriate). $\checkmark$
Award MP2 if 1.6 s (to give 50 m ) or 1.8 s (to give 56 m ) or 1.7 s (to give 53 m ) or average of two distances used
Allow 60 m.
(c) Use of $\mathrm{F}=\mathrm{ma}$ to calculate acceleration.
$a=6800 / 1200 \checkmark=5.7 \mathrm{~m} \mathrm{~s}^{-2}$
evidence of use of suvat to calculate s or $\mathrm{t}, \boldsymbol{\downarrow}$
to give $t=5.5 \mathrm{~s} \checkmark$
$s=85 \mathrm{~m} . \checkmark$
If no other mark given, allow 1 mark for
$m v=1200 \times 31$ (= 37200)
Alternative for MP1 and MP2
$t=\frac{m v-m u}{F}$
Allow ce for a.
Allow ce for either incorrects or $t$.
(d) (It is assumed that) the car in front would take the same time/travel the same distance as the car behind when braking/ only difference is reaction time of the driver of car behind. $\checkmark$ Or
Car in front cannot stop instantaneously (so car behind will have time/distance to bring car to rest).or words to that effect

Alternative:
suggestion that total stopping distance is too large (drivers would ignore it/inefficient use of motorway)
(e) Correct use of cos (5) $\checkmark$
E.g.
$m g=N \cos (5)$
Correct use of $\sin (5) \checkmark$
E.g.
$N \sin (5)\left(=m v^{2} / r\right)$
So
$m v^{2} / r$ seen $\checkmark$
And $v=(r g \tan (5))^{1 / 2}$
Gives $v=(200 \times 9.81 \times \tan (5))^{1 / 2}=13$
So speed limit $=13 \mathrm{~m} \mathrm{~s}^{-1} \checkmark$
May see cos (85) for sin (5)
Alternative for MP1 and MP2: Evidence of mg tan (5)
fourth mark is for answer and suggesting this as the speed limit.
Max 3 if $m g=N$ used
31. (a) Attempt to calculate weight of cage

Attempt to find vertical component of tension $T_{\mathrm{V}}$ in one rope eg $3.7 \times 10^{4} \cos 20$ or $3.5 \times 10^{4}$ seen $\checkmark$

Uses $F=$ twice their tension - their weight $\checkmark$
If weight not calculated, allow MP3 for doubling their tension or their resolved component
$5.8 \times 10^{4}(\mathrm{~N}) \checkmark$
(b) Use of $F=$ ma with $6 \times 10^{4} \mathrm{~N}$ or their (a) $\checkmark$ $50\left(\mathrm{~m} \mathrm{~s}^{-2}\right) \checkmark$

Allow $48\left(\mathrm{~m} \mathrm{~s}^{-2}\right)$.
(c) Calculation of length of rope
eg 35/cos20 or 37.2 seen $\checkmark$
Allow methods using $F=k \Delta L$ and $E=1 / 2 k \Delta L^{2}$
Calculation of extension of one rope or calculation of total extension of both ropes eg their length-24 or 13.2 or 26.4 seen $\checkmark$

Use of $E=1 / 2 F \Delta L$
e.g. $1 / 2 \times 3.7 \times 10^{4} \times 13.2=2.44 \times 10^{5}(\mathrm{~J}) \checkmark$
$4.9 \times 10^{5}(\mathrm{~J}) \checkmark$
(d) Use of $E$ lost $=\Delta E_{\mathrm{p}}$
eg $1.2 \times 10^{3} \times 9.81 \times \mathrm{h}=5 \times 10^{5} \mathrm{~V}$
No credit for use of suvat in either method and MP3 must come from correct Physics.
First method is for calculation of max $h$ and comparison with 50 m .
$h=42(\mathrm{~m}) \checkmark$
Allow h from their (c) if it rounds to $5 \times 10^{5}$
$42<50(\mathrm{~m})$, so claim not justified $\checkmark$
OR
Use of $\Delta E_{\mathrm{p}}=m g \Delta h$ with 50 m
eg $1.2 \times 10^{3} \times 9.81 \times 50 \checkmark$
Second method is for calculation of $\Delta E_{p}$ and comparison with $E$.
$\Delta E_{\mathrm{p}}=5.9 \times 10^{5}(\mathrm{~J}) \checkmark$
$5.9 \times 10^{5}>5 \times 10^{5}$, so claim not justified $\checkmark$
(e) $90 \mathrm{~km} \mathrm{~h}^{-1}=25 \mathrm{~m} \mathrm{~s}^{-1} \checkmark$

The conversion mark stands alone.

Use of $E_{\mathrm{k}}=1 / 2 m v^{2}$
eg $1 / 2 \times 1.2 \times 10^{3} \times(\text { their } v)^{2} \checkmark$
$3.8 \times 10^{5}(\mathrm{~J}) \checkmark$
ecf for their $v$
(f) If their $E_{\mathrm{k}}>5 \times 10^{5}$, claim is unjustified

## OR

If their $E_{\mathrm{k}}<5 \times 10^{5}$, claim may be justified depending on gain in $E_{\mathrm{p}}$ or losses due to resistive forces $\checkmark$
32. (a) 0.56 (N) $\checkmark$

1
(b) Definition of couple as two equal forces acting in opposite directions $\checkmark$ Moment of a couple is independent of the point about which moments are taken $\checkmark$

Forces (are equal but) don't act in opposite directions, therefore it is not correct $\checkmark$ Combined moment of the two forces depends on the point about which moments are taken, therefore not correct.
(c) Use of total upward force = total downward force

1 mark for any attempt to equate upward and downward forces. Response may be on diagram.
eg $0.87+0.62=1.12+W \checkmark$
0.32 (N) $\checkmark$

Attempt to use Principle of Moments $\checkmark$
0.14 (m) $\checkmark$

Allow MP4 if (their W) $\times($ their d $)=0.0448$
(d) Readings (on A and B) would be the same/1.44 (N) $\checkmark$
(Because) total downwards force/weight is same
OR
All (perpendicular) distances affected by the same factor
$(\cos \theta) \checkmark$

## (a) Method 1:

Attempts to determine area under curve / by counting squares ${ }_{1} \checkmark$
Multiplies their (total) area (or charge) by $24(\mathrm{~V})_{2} \sqrt{ }$
$240(J){ }_{3} \checkmark$
Allow POT error on area of square in ${ }_{1} \checkmark$ and ${ }_{2} \checkmark$
Evidence seen by calculations or from counting squares or from division of area into at least two recognisable geometrical shapes
(triangles, rectangles, trapezia)
answer in range 220 J to 264 J

## Method 2:

Attempt to determine average current (over first 200 ms in range 45 A to 55 A ) $1 \checkmark$
Use of $E=I \times V \times t_{2} \checkmark$
$240(J){ }_{3} \checkmark$
Substitutes current value (or $\Delta$ current) with $t=200 \mathrm{~ms}$ and $V=24$
V. Condone POT

Allow as two stage $Q=I t$ and $E=Q V$
$\operatorname{Or} P=V I$ and $E=P t$
answer in range 220 J to 264 J
(b) $\quad(\mathrm{KE}($ gained $)=) 65(.0)(\mathrm{J})$ or
$(P E($ gained $)=) 58(.3)(J)_{1} \downarrow$
Use of efficiency $=\frac{\text { an output energy }}{\text { ans from part } 0.1}$
Allow output energy $=65 / 58 / 120 / 123$ or candidate $k e+p e$
or (total output $=65+58=$ ) $123(\mathrm{~J})_{2} \sqrt{ } \sqrt{ }$
Allow ecf from (a) for all 3 marks.
(Efficiency =) 0.51 or $51 \%{ }_{3} \checkmark$
Answer to at least 2 sf. Range is 0.467 to 0.56 ( $46.7 \%$ to $56 \%$ )
(c) Heating occurs / temperature increases when there is a current (in the thermistor) (due to $I^{2} R$ ) $\sqrt{ } \checkmark$
(When the temperature increases) the resistance of thermistor decreases (whereas fixed resistor remains high) ${ }_{2} \sqrt{ }$
(Lower resistance from thermistor means) less wasted power ${ }_{3} \checkmark$
OR
(Lower resistance from thermistor means) more pd dropped across the motor (less wasted voltage) ${ }_{3} \checkmark$

Alternatively: (Lower resistance from the thermistor means) less voltage drop across thermistor ${ }_{3} \checkmark$
35. (a) The centre of mass of the beam and box is at the pivot $\checkmark$

Idea that moments balance / sum of the moments is zero at this position $\checkmark$

## OR

The anticlockwise moment (of weight of the beam) = clockwise moment (of weight of the box) $\checkmark$

Links pivot position to a consideration of moments $\checkmark$
Accept one route or the other, do not accept points from both.
Allow max 1 for "the pivot is to the right of the centre (of mass) of the beam"
'pivot' on its own does not get the first mark
Award 2 for $1.25 \times$ weight of beam $=1.5 \times$ weight of empty box
Confusion of moments with eg work done/forces = max 1
(b) Clockwise moment $=610 \times 9.81 \times 1.5(=8976 \mathrm{~N} \mathrm{~m}) \checkmark$

Anticlockwise moment $=250 \times 4+T \sin 50 \times 4.0(\mathrm{~N} \mathrm{~m}) \checkmark$
Use of clockwise = anticlockwise $\sqrt{ }$
Use of $T \sin 50^{\circ}$ seen / relates vertical component to tension $\checkmark$
$T\left(=1994 / \sin 50^{\circ}\right)=2600(\mathrm{~N}) \checkmark$
Credit any evidence to work out a moment with one mark Condone cos 50 in MP2.
Allow ecf for clockwise moment
Allow ecf for anticlockwise moment
Use of $g=10 \mathrm{Nkg}^{-1}$ gives 2990 N Omission of $4.0 \mathrm{~m}(\mathrm{~g}=9.8)$ gives 10410 N . Use of $\cos 50(g=9.8)$ gives 3100 N
Allow max 4 for use of $g=10 \mathrm{Nkg}^{-1}$.
(c) $7.5=1 / 2 \mathrm{~g} t^{2} \checkmark$
$(t=1.2 \mathrm{~s})$
(calculate distance)
$s(=u t=18 \times 1.2)=22(\mathrm{~m}) \checkmark$
Allow ecf from incorrect t for MP2
(d) (Range will be greater:)
component of velocity upwards $\checkmark$
rock will spend longer in the air $\checkmark$
greater $t \checkmark$
therefore the range is greater $\checkmark$
OR
(Range will be smaller)
Counterweight will fall less far before projectile released $\checkmark$
Less energy transferred to rock $\checkmark$
Initial speed of rock less/horizontal velocity reduced $\checkmark$
therefore the range is smaller $\checkmark$

## OR

(balanced arguments)
therefore the range is unchanged / answer is indeterminate $\checkmark$
Candidates can argue from both lists to reach a balanced view suggesting that there is no change.
Full credit can be obtained from 2 deductions from one list $\checkmark \checkmark+$ consistent conclusion $\checkmark$
1 deduction from each list $\checkmark \checkmark+$ consistent conclusion $\checkmark$
Do not allow an unsupported conclusion.
Conclusion must be consistent with correct statements.
Treat incorrect statements as neutral.
Do not reward arguments based on a longer time of flight.
36. (a) Conversion of $110 \mathrm{~km} \mathrm{~h}^{-1}$ to $31 \mathrm{~m} \mathrm{~s}^{-1} \checkmark$
$=1 / 2 \times 1.5 \times 10^{3} \times$ their conversion ${ }^{2}$ with a consistent answer $\checkmark$
$\left(=7(.2) \times 10^{5}\right)$
Allow ecf for incorrect or failure to carry out speed conversion
Expect answer to be calculated correctly and to 2+ sf.
Accept 700 kJ as 2 sf
(b) Component of velocity $=31 \times \cos (20)$

## OR

evidence of using momentum $=$ mass $\times$ velocity (eg $1.5 \times 10^{3} \times$ a velocity $) \checkmark$
$=4.4 \times 10^{4} \checkmark$
For unit only accept $\mathrm{kg} \mathrm{m} \mathrm{s}^{-1}$ OR $\mathrm{Ns} \checkmark$
Allow ecf for speed from part (a)
Accept $4.65 \times 10^{4} \mathrm{~kg} \mathrm{~m} \mathrm{~s}^{-1}$ for max 2
Use of $30.6 \mathrm{~m} \mathrm{~s}^{-1}$ gives 43 kN s
(c) (KE before collision $=700 \mathrm{~kJ}$ )

Speed (parallel to barrier) after $(=31 \times \cos 20)=28.7 \mathrm{~m} \mathrm{~s}^{-1} \checkmark$
KE $\operatorname{after}\left(=1 / 2 \times 1.5 \times 10^{3} \times 28.7^{2}\right)=618 \mathrm{~kJ} \checkmark$
Change $=700-618 \checkmark(=82 \mathrm{~kJ})$

## OR

Speed (perpendicular to barrier) after $=31 \times \sin 20\left(=10.5 \mathrm{~m} \mathrm{~s}^{-1}\right) \checkmark$
Loss of $\mathrm{KE}\left(=1 / 2 \times 1.5 \times 10^{3} \times 10.5^{2}\right)=82 \mathrm{~kJ} \checkmark$
Justification that total KE = KE due to speed parallel to barrier + KE due to speed perpendicular to barrier $\checkmark$

Allow ecf for speed from part (a)
Use of $K E=p^{2} / 2 m$ can gain full credit.
Allow ecf for momentum in part (b)
Final answer depends on extent to which candidate has rounded in earlier parts. Allow correctly evaluated solutions for full credit.
In this question, do not insist on final answer to 2+ sf.
If there is a suggestion that $K E$ is a vector or can be resolved, do not award MP3.
(d) Evidence of work done $=$ force $\times$ distance

Eg Force $=82000 / 1.5$ OR their value for part (c) $\div$ part (a) $\checkmark$
Allow 80 kJ for energy
$=5.5 \times 10^{4} \mathrm{~N} \checkmark$
This is less than braking force - so yes. $\checkmark$
OR energy approach

- work done by barrier $=60 \mathrm{kN} \times 1.5 \mathrm{~m}$ V
- $\quad 90 \mathrm{~kJ}$,
- which is $>\mathrm{E}_{\mathrm{k}}$ of vehicle, so yes $\checkmark$

OR impulse argument

- evaluate time taken to stop, $0.26 \mathrm{~s} \checkmark$
- impulse value leading to distance or force $\checkmark$
- conclusion consistent with correct method of calculation $\checkmark$

OR use of $F=$ ma and suvat :

- $F=$ ma leading to $a=(-) 40 \mathrm{~m} \mathrm{~s}^{-2} \checkmark$
- $\quad$ suvat leads to $1.37 \mathrm{~m} \checkmark$
- $\quad$ which is $<1.5 \mathrm{~m}$, so yes $\checkmark$

General scheme for alternatives and reverse arguments is:

- first step calculation
- subsequent calculation(s) leading to comparative value.

Allow ecf for error in first step.

- conclusion consistent with correct method of calculation

Alternative suvat method:

- uses suvat to get a $=36.5 \mathrm{~m} \mathrm{~s}^{-2}$
- uses $F=m a$
- which is <60 kN, so yes
(e) (Steel barrier is better because)

Increase time of contact as material deforms $\checkmark$
Reference to impulse (= change in momentum $=\mathrm{Ft}$ ) implies smaller force (on dummy) $\sqrt{ }$

OR
Increasing stopping distance as material deforms $\checkmark$

Reference to work done (= Fs) implies smaller force (on dummy) $\checkmark$
Allow correct discussion leading to concrete barrier is worse.
Alternative second mark for either alternative can be awarded for correct reference to $F=$ ma
39. A
40. A

